

# Analysis of low Power High Speed Design of Multipliers in CMOS Technologies

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**Abstract**— A processor central processing unit consumes a considerable amount of processing time in performing arithmetic operations, especially multiplication operations. Multiplication is one of the basic arithmetic operations and it requires more hardware resources and processing time than addition and subtraction. In fact, 9% of all the instruction in typical processing units is multiplication. In this paper, comparative study of different multipliers is done for low power requirement and high speed. Designing high speed and low power circuits with cmos technology have great importance in VLSI circuits. One of the efficient logics among the logic family is the constant delay (CD) logic style. In this paper CD logic has been modified and a new logic known as low power high speed (LP-HS) is proposed. With the help of three changes introduced in the CD logic style. LP-HS logic is developed which reduces the power delay product.

**Index Terms**— Multiplier, CMOS, VLSI, power consumption, constant delay logic (CD logic)

## I. INTRODUCTION

Multiplication is a fundamental function in arithmetic logic operations. DSP system's computational performance is limited by its multiplication performance [1] and multiplication dominates the execution time of most DSP algorithms [2] therefore high-speed multiplier is much desired [3]. Multiplication time is still the dominant factor in determining the instruction cycle time of a DSP chip. With an increasing need for greater computing power on battery-operated mobile devices, design emphasis has changed from optimizing conventional delay time area size to minimizing power dissipation while still keeping the high performance [4]. Normally shift and add algorithm has been implemented to design even though this is not suitable for VLSI implementation and also from delay point of view. Some of the important algorithm proposed in literature for VLSI implementable fast multiplication is Booth multiplier, array multiplier and Wallace tree multiplier [1]. This paper presents the fundamental technical aspects behind these approaches.

The low power and high speed VLSI can be implemented with different logic style. The three important considerations for VLSI design are power, area and delay [5-6]. High performance energy efficient logic style is having vital importance in VLSI circuits. CMOS is the dominant technology which is used to construct these type of integrated circuits. The three most widely accepted parameters to measure the quality of a circuit are area, delay and power. [12] Advances in CMOS technology have led to improvement in the performance in terms of area, power or delay. There is always a tradeoff between those in a circuit.

[13] The power delay product is a figure of merit for comparing logic circuit technologies or families.

Constant delay logic style is targeting at high speed applications. The constant delay characteristic of this logic style makes it suitable in implementing complicated logic expressions such as addition. The multipliers play a major role in arithmetic operations. In this paper both constant delay logic style as well as Low Power High Speed logic is analysed. [14]

## II. OBJECTIVES

The aim of good multiplier to provide a physically compact high speed and low power consumption unit. Being an important part of arithmetic processing unit, multipliers are in extremely high need on its speed and low power consumption. By reducing the number of operations thereby reducing a dynamic power return reduce significant power consumption of multiplier design as which is a major part of total power consumption.

## III. TECHNIQUES AND FUNCTIONS

Depending upon parameters such as latency, throughput and design complexity there are different techniques to perform binary multiplication. To sum partial products more efficient parallel approach uses some sort of array or tree of full adders. Array multiplier, booth multiplier and Wallace tree multipliers are some of the standard approaches to have hardware implementation of binary multiplier which are suitable for VLSI implementation at CMOS level.

To design low power, high speed circuits with CMOS technology have great importance in VLSI circuits. One of the efficient logics among the logic family is the constant delay (CD) logic style and other modified logic of the same is low power high speed (LP-HS) logic.

### 3.1 Array multiplier

Multiplication of two binary numbers can be obtained with one micro-operation by using a combinational circuit that forms the product bit all at once. Here delay is due to time for the signals to propagate through the gates that form the multiplication array thus achieving fast way of multiplying two numbers.

In array multiplier, consider two binary numbers A and B, of m and n bits. There are mn summands that are produced in parallel by a set of mn AND gates. n x n multiplier requires n(n-2) full adders, n half-adders and n<sup>2</sup> AND gates. Also, in array multiplier worst case delay would be (2n+1) td.

Array Multiplier gives more power consumption as well as optimum number of components required, but delay for this multiplier is larger. It is less economical [7][8] as it uses larger number of gates return area is also increased. Thus, it is a fast multiplier but hardware complexity is high [9].

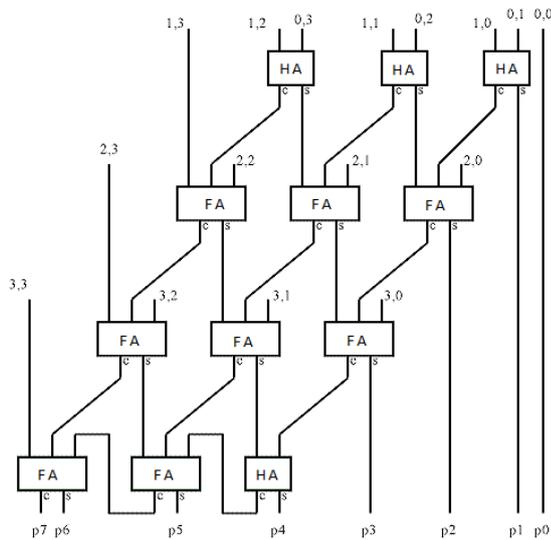


Fig 1. Array multiplier

3.2. Wallace tree multiplier

A fast process for multiplication of two numbers was developed by Wallace [10]. In this method, a three step process is used to multiply two numbers; the bit products are formed, the bit product matrix is reduced to a two row matrix where sum of the row equals the sum of bit products, and the two resulting rows are summed with a fast adder to produce a final product.

Three bit signals are passed to a one bit full adder (“3W”) which is called a three input Wallacetree circuit, and the output signal (sum signal) is supplied to the next stage full adder of the same bit, and the carry output signal thereof is passed to the next stage full adder of the same noof bit, and the carry output signal thereof is supplied to the next stage of the full adder located ata one bit higher position.

Wallace tree is a tree of carry-save adders arranged as shown in figure 2. A carry save adderconsists of full adders like the more familiar ripple adders, but the carry output from each bit isbrought out to form second result vector rather being than wired to the next most significantbit. The carry vector is 'saved' to be combined with the sum later. In the Wallace tree method,the circuit layout is not easy although the speed of the operation is high since the circuit is quiteirregular [7].

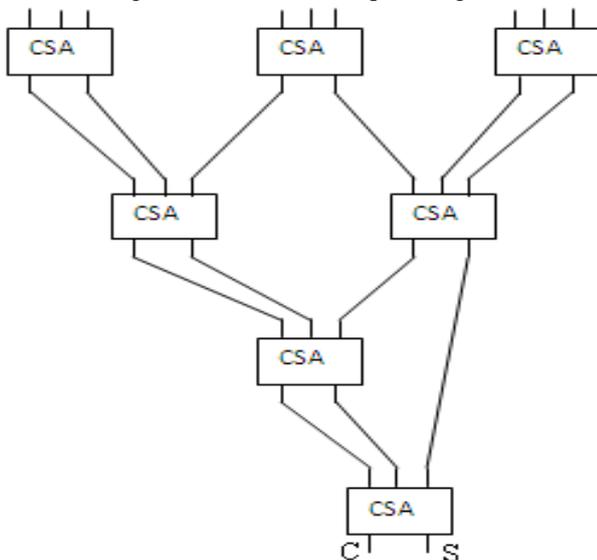


Fig 2. Wallace tree multiplier

3.3. Booth Multiplier

Another improvement in the multiplier is by reducing the number of partial products generated. The Booth recording multiplier is one such multiplier; it scans the three bits at a time to reduce the number of partial products [11]. These three bits are: the two bit from the present pair; and a third bit from the high order bit of an adjacent lower order pair. After examining each triplet of bits, the triplets are converted by Booth logic into a set of five control signals used by the adder cells in the array to control the operations performed by the adder cells.

To speed up the multiplication Booth encoding performs several steps of multiplication at once. Booth’s algorithm takes advantage of the fact that an adder subtractor is nearly as fast and small as a simple adder.

From the basics of Booth Multiplication it can be proved that the addition/subtraction operation can be skipped if the successive bits in the multiplicand are same. If 3 consecutive bits are same then addition/subtraction operation can be skipped. Thus in most of the cases the delay associated with Booth Multiplication are smaller than that with Array Multiplier. However the performance of Booth Multiplier for delay is input data dependant. In the worst case the delay with booth multiplier is on par with Array Multiplier [1].

The method of Booth recording reduces the numbers of adders and hence the delay required to produce the partial sums by examining three bits at a time. The high performance of booth multiplier comes with the drawback of power consumption. The reason is large number of adder cells required that consumes large power [11].

Table 1. Comparison between multipliers

Parameter	Array Multiplier	Wallace Tree multiplier	Booth’s Multiplier
Operation Speed	Less	High	Highest as the cycle length is as small as possible
Power consumption	Most	More	Less
Area	Maximum area as it uses a larger number of adders	Maximum area as wallace tree used to reduce operands	Minimum area because adder/subtractor is almost as small/fast as adder.
Complexity	Less complex	More complex	Most complex

IV. CONSTANT DELAY LOGIC STYLE

Due to the continuous demand of operating frequency, energy efficient logic style is always important in vlsi. This means that digital circuits needs high clock frequency to get fastest performance. Feed through logic (FTL) [15, 16, 17] is one of the efficient logics under c-mos dynamic domino logic. It has low dynamic power consumption and lesser delay when compared to other dynamic logic styles [18, 19, 20]. Static cmos logic circuits are less efficient as compared to dynamic logic circuits in terms of better speed and has lesser transistor requirement.

To solve the problems related with the feed through logic new high performance logic called constant delay (cd) logic has been designed. It performs with better energy efficiency compared to other logic styles. Complicated logic expressions are implemented by this high performance energy efficient logic style [21]

It exhibits a unique characteristic where the output is pre-evaluated before the input from the preceding stage is ready. Constant delay logic style which is used for high speed applications is shown in Fig 3.

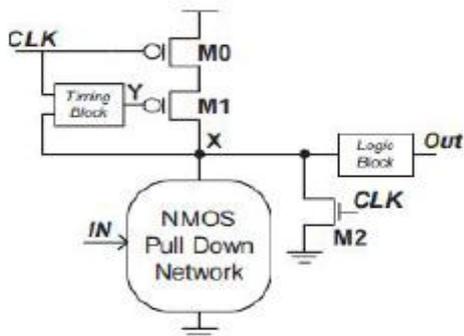


Fig 3: Constant Delay Logic Style [21]

CD logic consists of two extra blocks when compared to feedthrough logic. They are the timing block (TB) as well as the logic block (LB). Timing block consists of self reset technique and window adjustment technique. This enables robust logic operation with lower power consumption and higher speed. Logic block reduces the unwanted glitch and also makes cascading CD logic feasible. The unique characteristic of this logic is that the output is pre-evaluated before the inputs from the preceding stage got ready. An Nmos pull down network is placed where the inputs are given. Based on the logic which is given in the pull down network we will get the corresponding output. A buffer circuit implemented using CD logic is shown below. The expanded diagram for timing block as well as logic block is also shown in the Fig 4

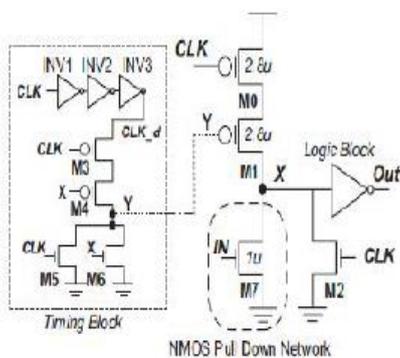


Fig 4: Buffer Using CD Logic [21]

The chain of inverters is acting as the local window technique and the NOR gate as a self reset circuit. Length of the inverter chain varies according to the circuit which we have to design. The prime aim of the inverter chain is to provide a delayed clock. The contention problem which is one of the disadvantages of the feedthrough logic is reduced with the help of this window adjustment. In the self reset circuit one of the input of the NOR gate is the intermediate output node X and the other one is the clock. The logic block is simply a static inverter as in the case of dynamic dominant logic. Since the above circuit is for a buffer the NMOS pull down network consists of only one nMOS transistor.

The timing diagram for constant delay logic is shown in Fig 5. CD logic works under two modes of operation.

- i. Pre-discharge mode (CLK=1)
- ii. Evaluation mode (CLK=0)

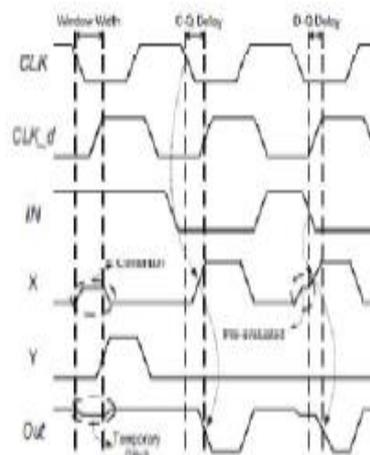


Fig 5: Timing Diagram of CD Logic [21]

Pre-discharge mode happens when CLK is high and evaluation mode occurs when CLK is low. During pre-discharge mode X and Out are pre-discharged and precharged to GND and VDD respectively. During evaluation mode three different conditions namely contention, C-Q delay and D-Q delay take place in the CD logic. Contention mode happens when IN=1 for the entire evaluation period. During this time a direct path current flows from pMOS to pDN. X rises to non-zero voltage level and Out experiences a temporary glitch. C-Q delay (clock-out) occurs when IN goes to 0 before CLK transits to low. At this time X rises to logic 1 and Out is discharged to VDD and the delay is measured from CLK to Out. D-Q delay happens when IN goes to 0 after CLK transits to low. During this time X initially enters contention mode and later rises to logic 1 and the delay is measured from IN to Out.

## V. PROPOSED LP-HS LOGIC

From the existing constant delay logic the proposed LP-HS logic is derived. In this logic there are three main differences when compared to CD-logic. There is no window adjustment technique. Instead, if an nMOS evaluation transistor and a pMOS transistor is used. Addition of transistors M2 and M3 in parallel below the pull-down network is the third variation. The proposed logic helps to reduce the power and delay which in turn reduces the power delay product. The circuit diagram for the proposed logic is shown in Fig 6

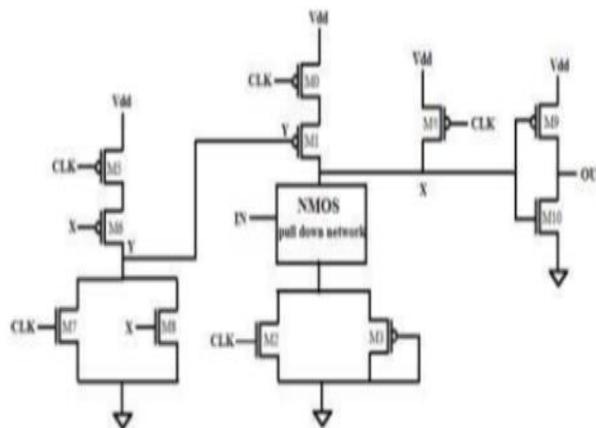


Fig 6: Proposed LP-HS Logic

The NOR gate which is behaving as the self resetting logic is constituted by the transistors M5,M6,M7 and M8.M5,M6,M7 and M8 is driven by clock and the output intermediate node X .Transistors M0 and M1 whose gates are driven by the CLK and the output of NOR gate are connected in series. This increases the resistance which in turn helps reducing the power. M4 is acting as an evaluation transistor. Transistors M2 and M3 are connected in parallel and is placed down to the nMOS pull down network. These transistors help to reduce the power delay product. The gate of M2 is driven by the clock and M3 is at ground. IN values are given to the nMOS pull down network which is given according to the circuit which we have to design. The dynamic resistance of the pull down network is increased by transistor M2 which in turn helps to reduce the power consumption. Transistors M9 and M10 together figures the static inverter which is used to make the cascading logic more feasible.

The circuit works under two modes of operation.

- i. Precharge mode (CLK=0)
- ii. Evaluation mode (CLK=1)

Evaluation mode happens when clock is high and precharge mode occurs when clock is low. When clock is low,transistor M4 gets ON and provides a high value at node X which in turn provides a low value at the output node OUT.

When clock is high the transistor M2 gets ON and the nMOS pull down network is evaluated and gives the output. During this time the transistor M0 whose gate is driven by the CLK is in OFF condition. Due to this the contention mode gets wiped out in the evaluation condition which in turn tends for the elimination of window adjustment technique in the proposed logic. One of the reasons for the power and delay reduction in the circuit is the elimination of the window adjustment technique. During the evaluation mode the pull down network and the transistor M2 gets ON which provides high dynamic resistance which further reduces the power. Transistor M3 is in always ON condition which offers an easy discharge of the value to the ground.

## VI. CONCLUSION

Array multiplier requires more power consumption and gives maximum number of components required ,but delay for this multiplier is more than wallace tree multiplier. Booth multiplier is superior in all aspects like delay,speed,area,complexity and power consumption. Therefore it can be concluded that for low power requirement and less delay requirement booths multiplier is suggested.

The new logic called LP-HS logic is developed by modifying constant logic delay multipliers are designed using both existing as well as proposed logic.

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